

# Alternating Current

Instantaneous value of alternating current at any instant of time

$$I = I_0 \sin \omega t$$

$I_0$  = peak value of alternating current

Root Mean Square Value of Alternating Current

$$I_{rms} = \sqrt{\frac{\int I^2 dt}{\int dt}}$$

$$I_{rms} = \frac{I_0}{\sqrt{2}}$$

$$V_{rms} = \frac{V_0}{\sqrt{2}}$$

## Impedance

The opposition offered by an AC circuit containing more than one out of three components L, C and R is called impedance (Z) of the circuit.

Impedance of an AC circuit,

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

Power of an AC Circuit

$$P_{av} = V_{rms} I_{rms} \cos \theta$$

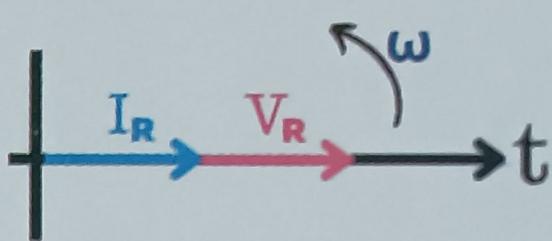
Where  $\cos \theta = \frac{\text{Resistance}}{\text{Impedance}}$

A/C	Sinusodial A/C	Square A/C	Triangular
$(Avg)_{full}$	0	0	0
$(Avg)_{half}$	$\frac{2I_0}{\pi}$	$I_0$	$\frac{I_0}{2}$
r.m.s.	$\frac{I_0}{\sqrt{2}}$	$I_0$	$\frac{I_0}{\sqrt{3}}$

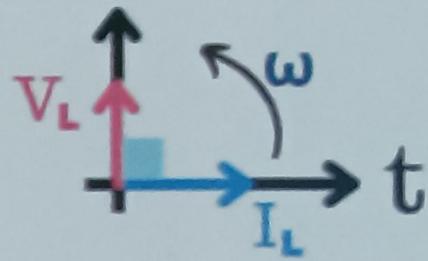
Circuit	Phase Difference between I and V	Power Factor $\cos \phi = \frac{R}{Z}$	Impedence	Who Leads	Power Loss
Pure Resistive	Zero	1	R	Same Phase	$P = I_{rms} = V_{rms}$
Pure Capacitive	$\frac{\pi}{2}$	Zero	$\chi_C = \frac{1}{\omega C}$	Current	Zero
Pure Inductive	$\frac{\pi}{2}$	Zero	$\chi_L = \omega L$	Voltage	Zero
R-L	$0 < \phi < \pi/2$	Between 0 and 1	$\sqrt{R^2 + \chi_L^2}$	Voltage	$P = I_{rms} \frac{R}{Z}$
R-C	$0 < \phi < \pi/2$	Between 0 and 1	$\sqrt{R^2 + \chi_C^2}$	Current	
L-C	$\pi/2$	Zero	$\chi_L - \chi_C$	Depends	

# Phasor Diagrams for different AC Circuits

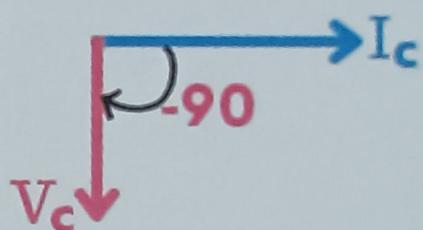
## Pure Resistive



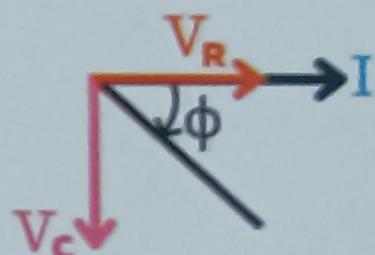
## Pure Inductive



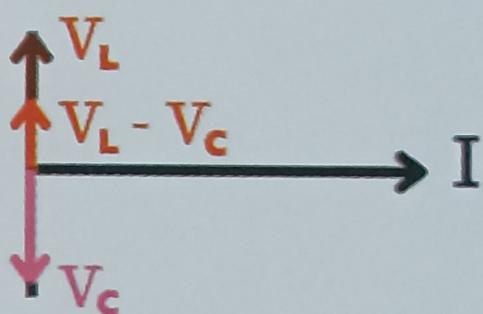
## Pure Capacitive



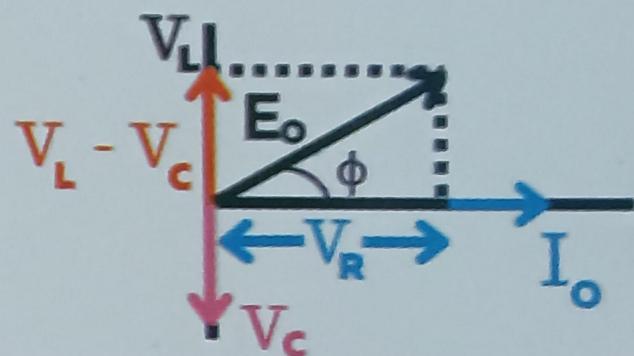
## R-C



## L-C



## L-C-R



## Resonance in AC Circuit

The condition in which current is maximum or impedance is minimum or vice-versa in an AC circuit is called resonance.

### Series Resonance Circuit

At resonance,

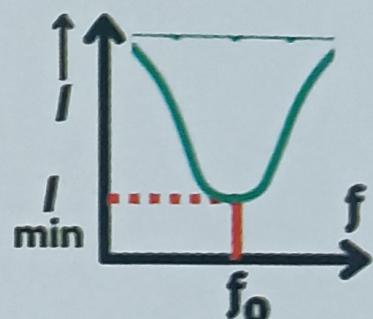
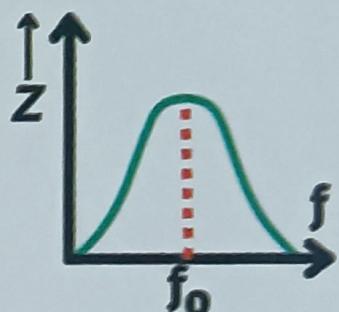
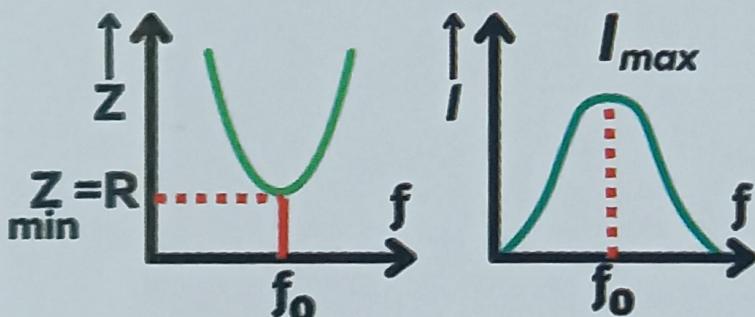
$$\chi_L = \chi_C$$

Resonance frequency,

$$f = \frac{1}{2\pi\sqrt{LC}}$$

Q factor or sharpness at resonance,

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$



LC Oscillation  $\rightarrow$  Energy Conserved

$$(U_C + U_L)_{initial} = (U_C + U_L)_{final}$$

## Transformer

**Ratio of Secondary and Primary Voltage**  
where  $N_P$  and  $N_S$  are number of turns in primary and secondary coil respectively

$$\frac{V_S}{V_P} = \frac{N_S}{N_P}$$

**Ratio of Secondary and Primary Current**

$$\frac{I_S}{I_P} = \frac{N_P}{N_S}$$

## Step up Transformer

### Primary Coil

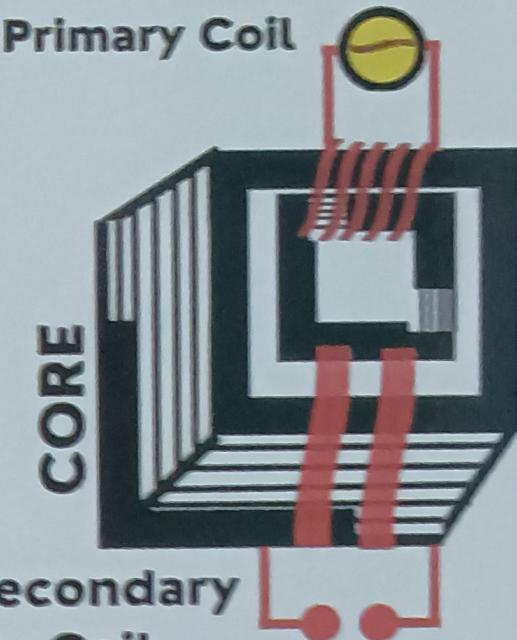


### Secondary Coil

$$\begin{aligned}V_{\text{output}} &> V_{\text{input}} \\N_S &> N_P \\I_S &< I_P \\P_{\text{input}} &= P_{\text{output}}\end{aligned}$$

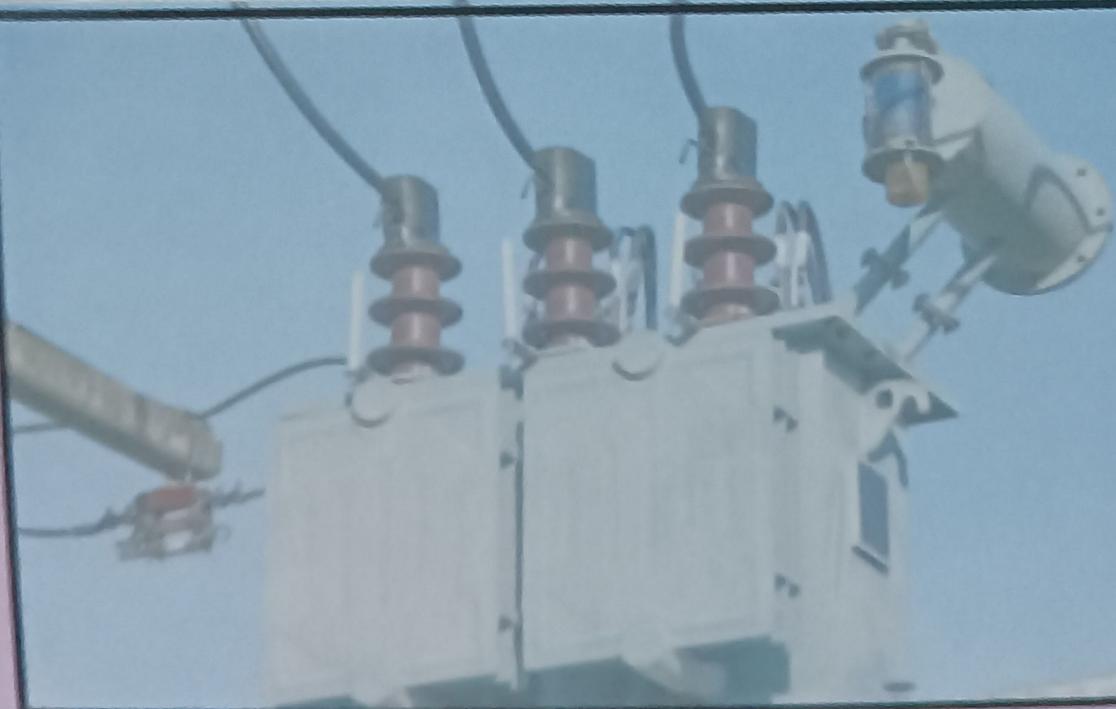
## Step down Transformer

### Primary Coil



### Secondary Coil

$$\begin{aligned}V_{\text{output}} &< V_{\text{input}} \\N_S &< N_P \\I_S &> I_P \\P_{\text{input}} &= P_{\text{output}}\end{aligned}$$



- In a series LCR circuit, the inductance L is  $10 \text{ mH}$ , capacitance C is  $1 \mu\text{F}$  and resistance R is  $100 \Omega$ . The frequency at which resonance occurs is : **1.59 kHz**
- The net magnetic flux through any closed surface is : **Zero**
- A  $12 \text{ V}, 60 \text{ W}$  lamp is connected to the secondary of a step down transformer, whose primary is connected to ac mains of  $220 \text{ V}$ . Assuming the transformer to be ideal, what is the current in the primary winding : **0.27A**
- An ac source is connected to a capacitor C. Due to decrease in its operating frequency : **Displacement Current Decreases**
- The magnetic energy stored in an inductor of inductance  $4 \mu\text{H}$  carrying a current of  $2 \text{ A}$  is :  **$8 \mu\text{J}$**
- The net impedance of circuit (as shown in figure) will be :  **$5\sqrt{5}\Omega$**

