

# Alternating Current

**Instantaneous value of alternating current at any instant of time**

$$I = I_0 \sin \omega t$$

$I_0$  = peak value of alternating current

**Root Mean Square Value of Alternating Current**

$$I_{rms} = \sqrt{\frac{\int I^2 dt}{\int dt}}$$

$$I_{rms} = \frac{I_0}{\sqrt{2}}$$

$$V_{rms} = \frac{V_0}{\sqrt{2}}$$

**Impedance**

The opposition offered by an AC circuit containing more than one out of three components L, C and R is called impedance (Z) of the circuit.

Impedance of an AC circuit,

$$Z = \sqrt{R^2 + (\chi_L - \chi_C)^2}$$

**Power of an AC Circuit**

$$P_{av} = V_{rms} I_{rms} \cos \theta$$

Where  $\cos \theta = \frac{\text{Resistance}}{\text{Impedance}}$





A/C	Sinusodial A/C	Square A/C	Triangular
$(Avg)_{full}$	0	0	0
$(Avg)_{half}$	$\frac{2I_0}{\pi}$	$I_0$	$\frac{I_0}{2}$
r.m.s.	$\frac{I_0}{\sqrt{2}}$	$I_0$	$\frac{I_0}{\sqrt{3}}$

Circuit	Phase Difference between I and V	Power Factor $\cos \phi = \frac{R}{Z}$	Impedence	Who Leads	Power Loss
Pure Resistive	Zero	1	R	Same Phase	$P = I_{rms} V_{rms}$
Pure Capacitive	$\frac{\pi}{2}$	Zero	$X_C = \frac{1}{\omega C}$	Current	Zero
Pure Inductive	$\frac{\pi}{2}$	Zero	$X_L = \omega L$	Voltage	Zero
R-L	$0 < \phi < \pi/2$	Between 0 and 1	$\sqrt{R^2 + X_L^2}$	Voltage	$P = I_{rms} R = V_{rms} \frac{R}{Z}$
R-C	$0 < \phi < \pi/2$	Between 0 and 1	$\sqrt{R^2 + X_C^2}$	Current	
L-C	$\pi/2$	Zero	$X_L - X_C$	Depends	



# Phasor Diagrams for different AC Circuits

Pure Resistive	Pure Inductive
Pure Capacitive	R-C
L-C	L-C-R



## Resonance in AC Circuit

The condition in which current is maximum or impedance is minimum or vice-versa in an AC circuit is called resonance.

### Series Resonance Circuit

At resonance,

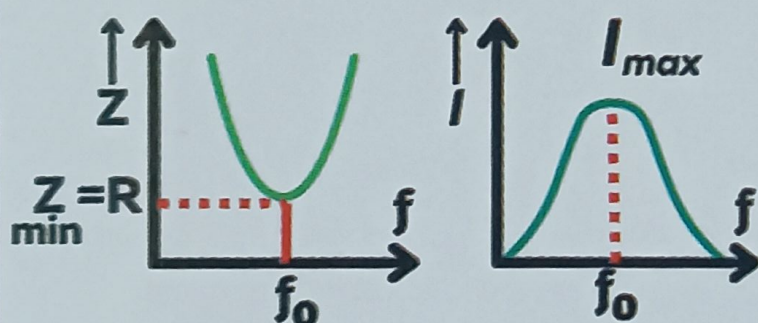
$$\chi_L = \chi_C$$

Resonance frequency,

$$f = \frac{1}{2\pi\sqrt{LC}}$$

Q factor or sharpness at resonance,

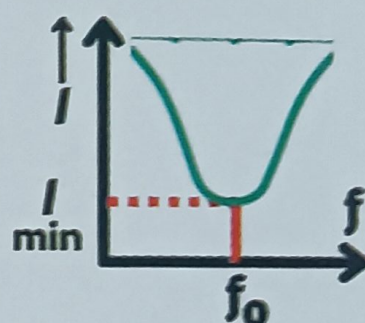
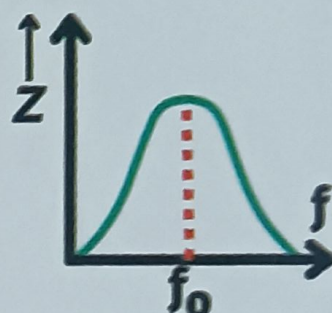
$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$



### Parallel Resonance Circuit

At resonance,

$$\chi_L = \chi_C$$



**LC Oscillation → Energy Conserved**

$$(U_C + U_L)_{\text{initial}} = (U_C + U_L)_{\text{final}}$$

## Transformer

**Ratio of Secondary and Primary Voltage**  
where  $N_P$  and  $N_S$  are number of turns in primary and secondary coil respectively

$$\frac{V_S}{V_P} = \frac{N_S}{N_P}$$

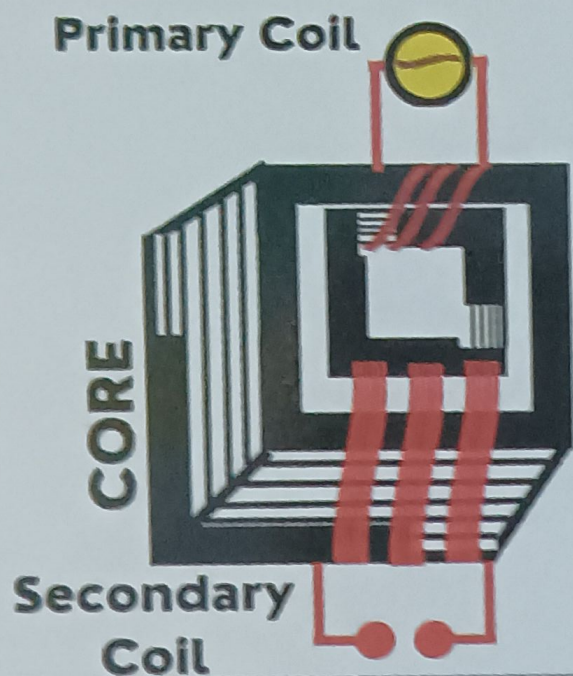
**Ratio of Secondary and Primary Current**

$$\frac{I_S}{I_P} = \frac{N_P}{N_S}$$





### Step up Transformer



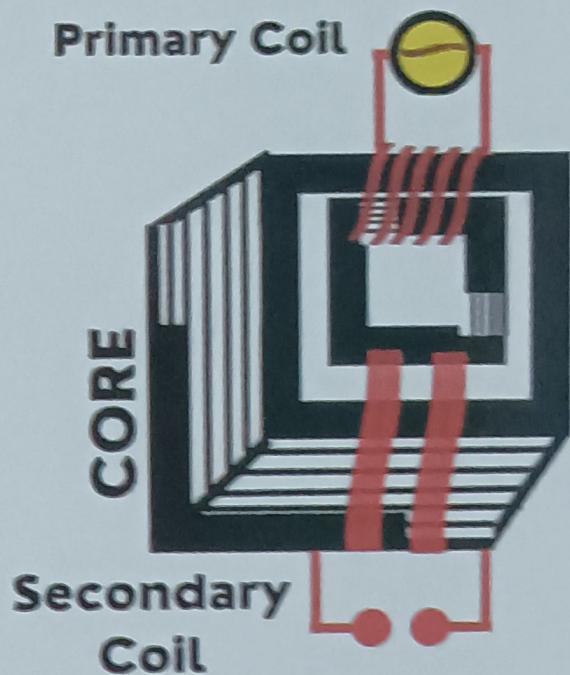
$$V_{\text{output}} > V_{\text{input}}$$

$$N_S > N_P$$

$$I_S < I_P$$

$$P_{\text{input}} = P_{\text{output}}$$

### Step down Transformer

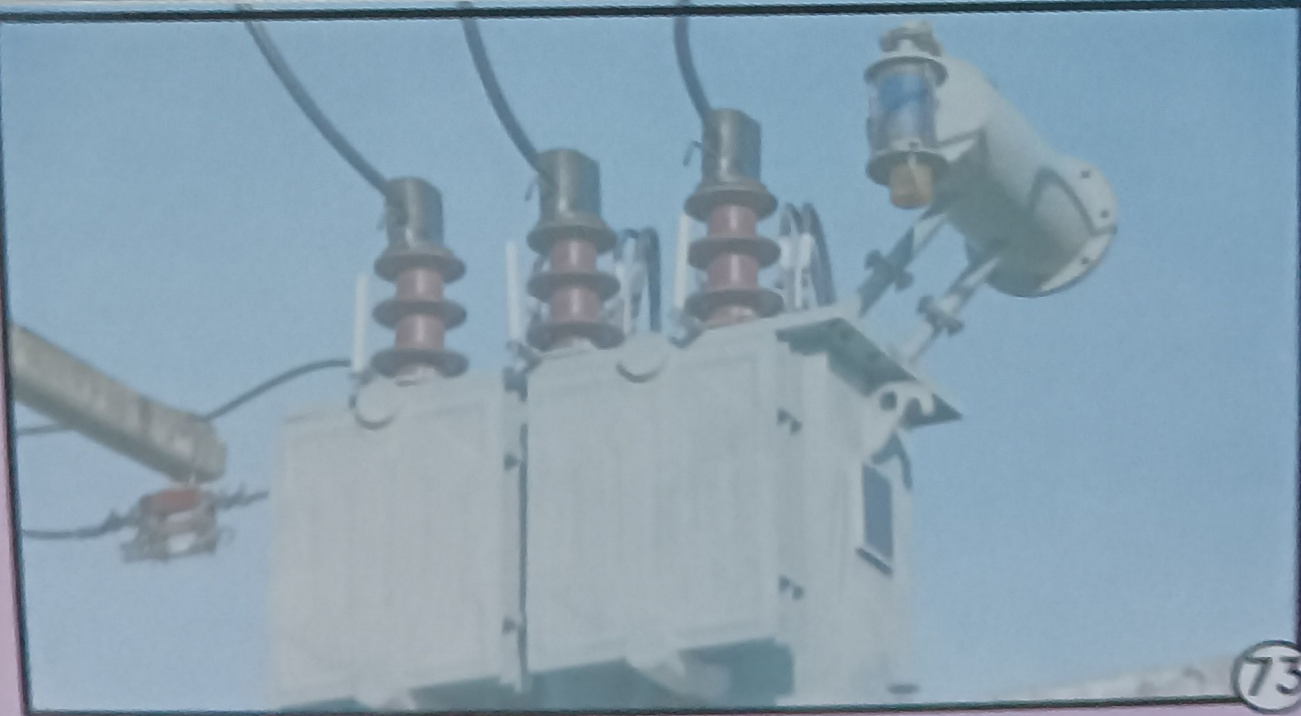


$$V_{\text{output}} < V_{\text{input}}$$

$$N_S < N_P$$

$$I_S > I_P$$

$$P_{\text{input}} = P_{\text{output}}$$





## NEET 2023 PYQ'S (Chapter 17-18)

- In a series LCR circuit, the inductance  $L$  is  $10\text{ mH}$ , capacitance  $C$  is  $1\text{ }\mu\text{F}$  and resistance  $R$  is  $100\text{ }\Omega$ . The frequency at which resonance occurs is :  **$1.59\text{ kHz}$**
- The net magnetic flux through any closed surface is : **Zero**
- A  $12\text{ V}, 60\text{ W}$  lamp is connected to the secondary of a step down transformer, whose primary is connected to ac mains of  $220\text{ V}$ . Assuming the transformer to be ideal, what is the current in the primary winding :  **$0.27\text{ A}$**
- An ac source is connected to a capacitor  $C$ . Due to decrease in its operating frequency : **Displacement Current Decreases**
- The magnetic energy stored in an inductor of inductance  $4\text{ }\mu\text{H}$  carrying a current of  $2\text{ A}$  is :  **$8\text{ }\mu\text{J}$**
- The net impedance of circuit (as shown in figure) will be :  **$5\sqrt{5}\Omega$**

